

# Lecture 10

## Topics in Development Economics: Household Models

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# Motivation

- Most people in developing countries earn part of their livelihood through work in their own enterprises.
- Moreover, they consume a portion of the output of their productive activities.
- Household labor is an important input into the production process of the enterprise.  
⇒ Individuals make simultaneous decisions about:
  - *production*:
    - the level of output;
    - the demand for factors;
    - the choice of technology.
  - *consumption*:
    - labor supply;
    - commodity demand.

## Agricultural household model:

a model of the household that is jointly engaged in production and consumption.

# AHM under Complete Markets

Consider a household with 2 members, each of whom gets utility from:

- consuming a good ( $c_1$  and  $c_2$ );
- leisure ( $l_1$  and  $l_2$ ).

Each household faces a complete set of competitive markets.

Let:

- $p$ : the price of output;
- $w$ : the wage of labor;
- $F(L, A)$ : a concave production function:
  - $A$ : area of the farm cultivated by the household;
  - $L$ : amount of labor used on the farm.
- $E_i^L$ : person  $i$ 's endowment of time;
- $E^A$ : household's endowment of land;
- $r$ : the price of one unit of land.

# AHM under Complete Markets

The household's problem is to solve

$$\text{Max } U(c_1, c_2, l_1, l_2) \quad (1)$$

subject to

$$p(c_1 + c_2) + wL^h + rA^h \leq F(L, A) + w(L_1^m + L_2^m) + rA^m \quad (2)$$

$$L = L_1^f + L_2^f + L^h \quad (3)$$

$$A = A^f + A^h \quad (4)$$

$$E^A = A^f + A^m, \quad E_i^L = L_i^f + L_i^m + l_i, \quad i \in \{1, 2\} \quad (5)$$

$$c_i, l_i, L_i^f, L_i^m, A^f, A^m \geq 0, \quad i \in \{1, 2\}. \quad (6)$$

# AHM under Complete Markets

Substituting (3)-(5) into (2), we find:

$$p(c_1 + c_2) + w(l_1 + l_2) \leq \Pi + w(E_1^L + E_2^L) + rE^A \quad (7)$$

$$\Pi = F(L, A) - wL - rA \quad (8)$$

$$c_i, l_i, L, A \geq 0, \quad i \in \{1, 2\}. \quad (9)$$

The household's problem is now to maximize (1) (with respect to  $L, A, c_i$  and  $l_i$ ) subject to (7)-(9).

# AHM under Complete Markets

$L$  and  $A$  do not appear in (1), hence (1) and (7) can be replaced with

$$\max_{\{c_i\}, \{l_i\}} U(c_1, c_2, l_1, l_2) \quad (1')$$

subject to

$$p(c_1 + c_2) + w(l_1 + l_2) \leq \Pi^*(w, r) + w(E_1^L + E_2^L) + rE^A \quad (7')$$

where

$$\Pi^*(w, r) = \max_{L, A} F(L, A) - wL - rA. \quad (8')$$

The transformation of the problem reveals the fact that the household's production decisions are characterized by a simple profit maximization condition (8').



# AHM under Complete Markets

- Households choose labor and land inputs so as to maximize profit.
- Production decisions made on any plot depend only on prices and the characteristics of that plot, not on the household's endowments or preferences.

## Separation property of the agricultural household model:

the production decisions of the household are separable from the household's consumption choices.

The separation property is robust to the non-existence of some markets:

- If there is no land market;
- If there is no labor market.

# AHM under Complete Markets

Suppose that  $U(.)$  is such that all prices and wages

- $c_1 = c_2 = c$ ;
- $l_1 = l_2 = l$ .

Assuming that there is no market for land, the household chooses  $c$ ,  $l$ , and  $L$ .

The household's decision-making process proceeds in two stages:

- 1 Farm profit is maximized.
- 2 Utility is maximized given the full income budget constraint.

# AHM under Complete Markets

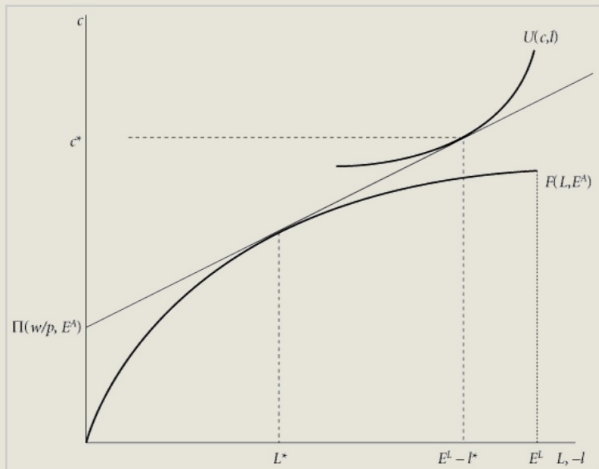


Figure 2.1

*But are the markets complete?*

# AHM under Complete Markets

- In most developing countries where the hypothesis has been examined it is clear that the separation property does not hold.
- Everywhere in Africa, Latin America, and most of Asia where the hypothesis has been examined, it has decisively been rejected:
  - Kevane (1994);
  - Udry (1998);
  - Barrett (1996);
  - Collier (1983);
  - Jacoby (1993);
  - Carter (1984);
  - Bardhan (1973).

⇒ Farmers *do not* maximize profits; their production decisions are related to their preferences and endowments.

# AHM under Incomplete Markets

If multiple markets are incomplete, the separation property no longer holds:

- The household no longer maximizes profit;
- Production decisions depend upon the preferences and endowments of the household.

Suppose that there is

- no market for land;
- some involuntary unemployment in the rural labor market.

The household cultivates its endowment of land, and might face a binding constraint on the amount of labor it can supply off its own farm.

# AHM under Incomplete Markets

The household problem (now assuming just one person in the household) is:

$$\max_{c, l, L^h, L^f \geq 0} U(c, l) \quad (10)$$

subject to

$$pc = F(L^f + L^h, E^A) - wL^h + wL^m \quad (11)$$

$$l + L^f + L^m = E^L \quad (12)$$

$$L^m \leq M \quad (13)$$

where

- $L^h$  is labor hired by the household to work on its farm;
- $L^f$  is the household's own labor on its farm;
- $L^m$  is the time spent by the household working for a wage;
- $M$  is the maximum amount of time the household can spend working for a wage as a result of some labor market rationing.

# AHM under Incomplete Markets

In this case,  $L^m = M$ ,  $L^h = 0$

Setting the numeraire  $p = 1$ , the household's problem becomes

$$\max_{c, l \geq 0} U(c, l) \quad (14)$$

subject to

$$c = F(E^L - M - l, E^A) + wM \quad (15)$$

- Then, the household's production choice depends on its preferences and its endowment.
- The separation property does not hold.



# AHM under Incomplete Markets

This sort of market structure could give rise to an often observed pattern in rural areas of less developed countries:

- Small farms are often cultivated more intensively than large farms.
- More labor per unit area is used on small farms.
- Yields are larger on these smaller farms.

# AHM under Incomplete Markets

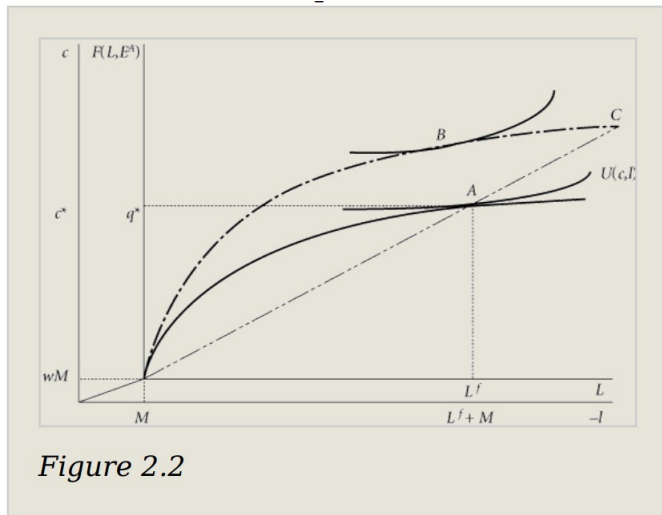


Figure 2.2

# Unitary Household Model

## Unitary model of the household:

household as a single decision-making agent, with a single budget constraint, and maximizing a unique utility function in which each household member's consumption enters as an argument.

In other words, *households* behave as if they are single *individuals*. Put another way, all resources are pooled and then reallocated according to some common rule.

# Unitary Household Model

*But is the household unitary?*

# Unitary Household Model

- Starting from the 1980s the unitary model of the household has been criticized on both the theoretical and empirical grounds.
- The *household* is not an *individual*. Why would the decision of the individuals within the household be made like those of one individual?
  - ① *What are the specific cases when a household may act like one individual when making decisions?*
  - ② *Why do we care about how decisions are made and how resources are allocated within the household?*

# Unitary Household Model

- Starting from the 1980s the unitary model of the household has been criticized on both the theoretical and empirical grounds.
- The *household* is not an *individual*. Why would the decision of the individuals within the household be made like those of one individual?
  - ① *What are the specific cases when a household may act like one individual when making decisions?*
    - "Dictatorial" household;
    - Household with "unanimous" preferences.
  - ② *Why do we care about how decisions are made and how resources are allocated within the household?*
    - It is important to design effective policies and to evaluate the impact of these policies on outcomes (such as poverty alleviation, educational achievement, etc.)

# Unitary Household Model

- In the unitary model, aggregate demand does not depend on the distribution of income within the household.
- However, a growing number of studies have found evidence that the budget shares of particular goods are significantly related to the shares of income accruing to women in the household.
  - *Example:* Thomas (1991) finds that in Brazil the unearned income of mothers has a much stronger positive effect on child health than the unearned income of fathers, contradicting the unitary household model.

# Nash Cooperative Bargaining Models

- As a result, alternative models of household behavior have been proposed in the literature:
  - *Example:* Nash cooperative bargaining models.
    - One assumption of these models is that the allocation of resources within a household is *Pareto efficient*.
    - The particular Pareto-efficient allocation that is chosen is determined by the *threat points* of the individual members of the household.

## Threat point

of an individual is defined as the utility achieved by that person if the household does not come to an agreement regarding the distribution of resources.

- ③ *What is **Pareto efficiency**?*



# Nash Cooperative Bargaining Models

- As a result, alternative models of household behavior have been proposed in the literature:
  - *Example:* Cooperative bargaining models.
    - One assumption of these models is that the allocation of resources within a household is *Pareto efficient*.
- ③ **What is Pareto efficiency?**

## Pareto efficiency (Pareto optimality)

a situation where no individual or preference criterion can be better off without making at least one individual or preference criterion worse off.

- But there are clear examples against Pareto efficiency in households.
    - *Example:* domestic violence against women and children.
    - *Example:* Udry (1996) finds that women's plots are cultivated much less intensively than their husbands' plots in parts of Burkina Faso.
      - It implies that total agricultural output within the household could be increased by reallocating factors of production across the plots cultivated by household members.
- ⇒ This contradicts the Pareto efficiency of resource allocation.

# Summary

- The available empirical evidence casts serious doubt on the validity of the unitary model.
- While the available work is mostly supportive of the more general model of efficient households, there is some evidence, particularly in Africa, that calls even this weaker model into question.
- More research is required before the general validity of the efficient household model can be accepted.
- If the efficient household model cannot adequately account for the intra-household allocation of resources, it appears that it will be necessary to move towards more detailed, culturally and institutionally informed noncooperative models of the interaction between household members.

- Bardhan, P., & Udry, C. (1999). Chapter 2. Development Microeconomics. Oxford University Press.  
<https://doi.org/10.1093/0198773714.001.0001>