

**CHAPTER FIFTEEN**  
**Consumption**

macroeconomics

# Chapter overview

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This chapter surveys the most prominent work on consumption:

- John Maynard Keynes: consumption and current income
- Irving Fisher and Intertemporal Choice
- Franco Modigliani: the Life-Cycle Hypothesis
- Milton Friedman: the Permanent Income Hypothesis

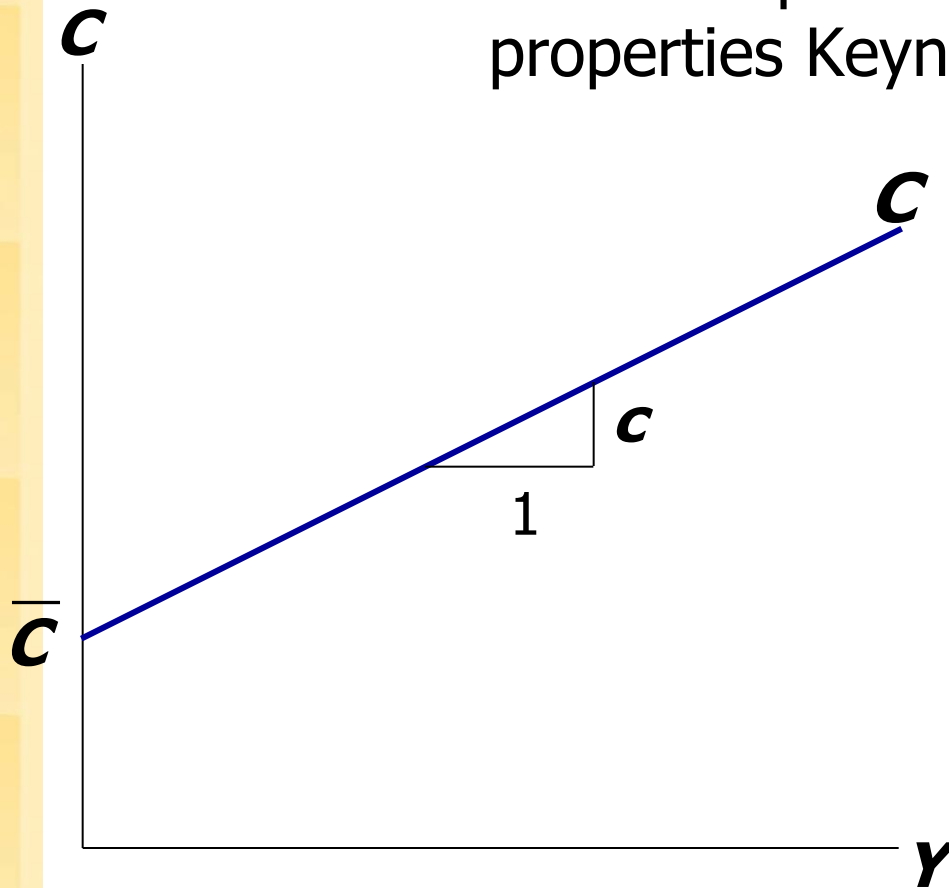
# Keynes's Conjectures

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1.  $0 < MPC < 1$
2.  $APC$  falls as income rises  
where  $APC$   
= **average propensity to consume**  
=  $C/Y$
3. Income is the main determinant of consumption.

# The Keynesian Consumption Function

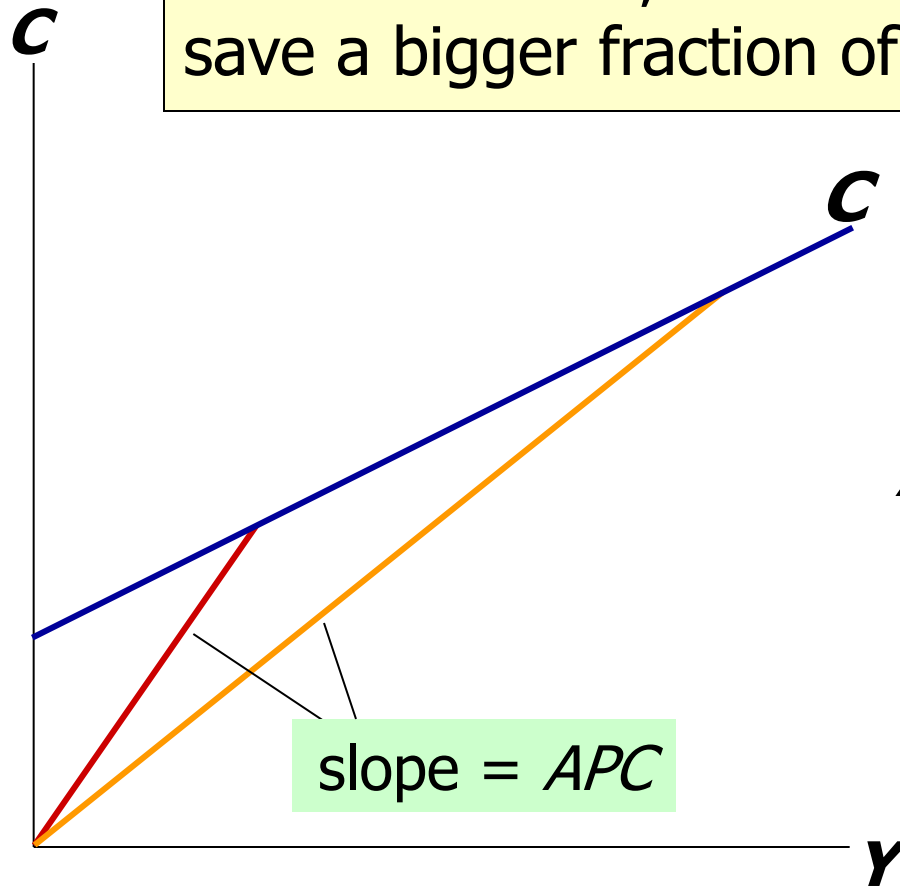
A consumption function with the properties Keynes conjectured:



$c = MPC$   
= slope of the  
consumption  
function

# The Keynesian Consumption Function

As income rises, the APC falls (consumers save a bigger fraction of their income).



$$APC = \frac{C}{Y} = \frac{\bar{C}}{Y} + c$$

# Early Empirical Successes: Results from Early Studies

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- Households with higher incomes:
  - consume more  
⇒  $MPC > 0$
  - save more  
⇒  $MPC < 1$
  - save a larger fraction of their income  
⇒  $APC \downarrow$  as  $Y \uparrow$
- Very strong correlation between income and consumption  
⇒ income seemed to be the main determinant of consumption

# *Problems for the Keynesian Consumption Function*

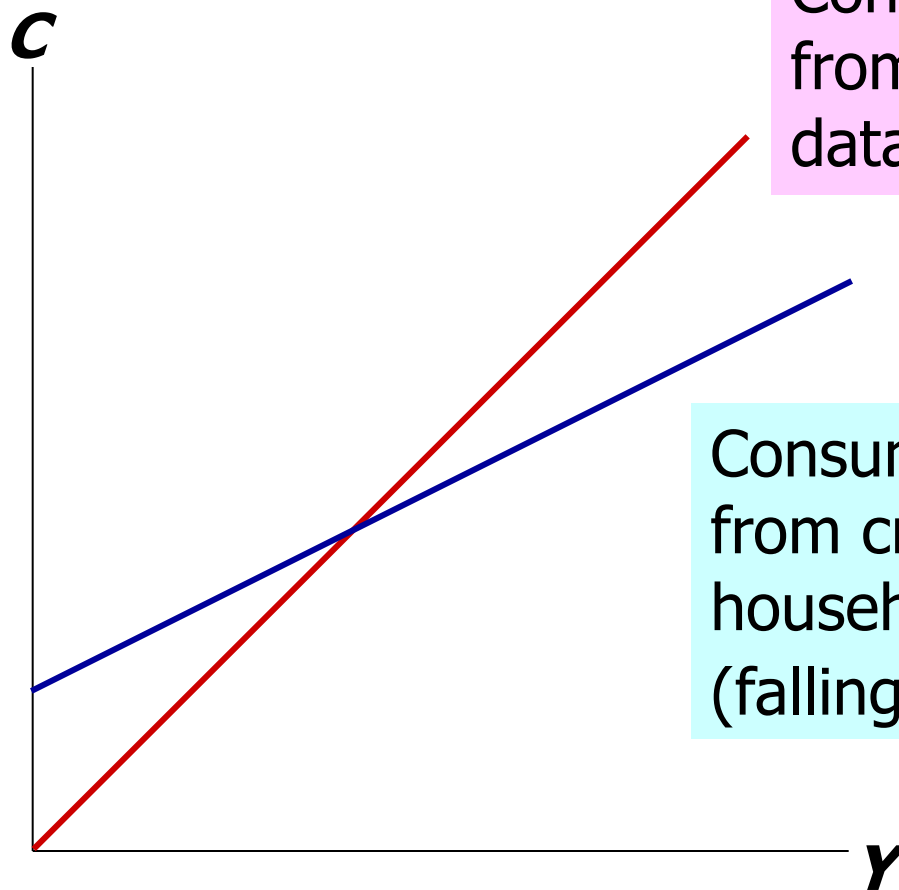
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Based on the Keynesian consumption function, economists predicted that  $C$  would grow more slowly than  $Y$  over time.

This prediction did not come true:

- As incomes grew, the APC did not fall, and  $C$  grew just as fast.
- Simon Kuznets showed that  $C/Y$  was very stable in long time series data.

# The Consumption Puzzle



Consumption function  
from long time series  
data (constant  $APC$ )

Consumption function  
from cross-sectional  
household data  
(falling  $APC$ )



# Irving Fisher and Intertemporal Choice

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- The basis for much subsequent work on consumption.
- Assumes consumer is forward-looking and chooses consumption for the present and future to maximize lifetime satisfaction.
- Consumer's choices are subject to an **intertemporal budget constraint**, a measure of the total resources available for present and future consumption

# The basic two-period model

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- Period 1: the present
- Period 2: the future
- Notation

$Y_1$  is income in period 1

$Y_2$  is income in period 2

$C_1$  is consumption in period 1

$C_2$  is consumption in period 2

$S = Y_1 - C_1$  is saving in period 1

( $S < 0$  if the consumer borrows in period 1)

# Deriving the intertemporal budget constraint

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- Period 2 budget constraint:

$$\begin{aligned}\mathbf{C}_2 &= \mathbf{Y}_2 + (1 + r)\mathbf{S} \\ &= \mathbf{Y}_2 + (1 + r)(\mathbf{Y}_1 - \mathbf{C}_1)\end{aligned}$$

- Rearrange to put  $\mathbf{C}$  terms on one side and  $\mathbf{Y}$  terms on the other:

$$(1 + r)\mathbf{C}_1 + \mathbf{C}_2 = \mathbf{Y}_2 + (1 + r)\mathbf{Y}_1$$

- Finally, divide through by  $(1+r)$ :

# The intertemporal budget constraint

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$$c_1 + \frac{c_2}{1+r} = y_1 + \frac{y_2}{1+r}$$

present value of  
lifetime consumption

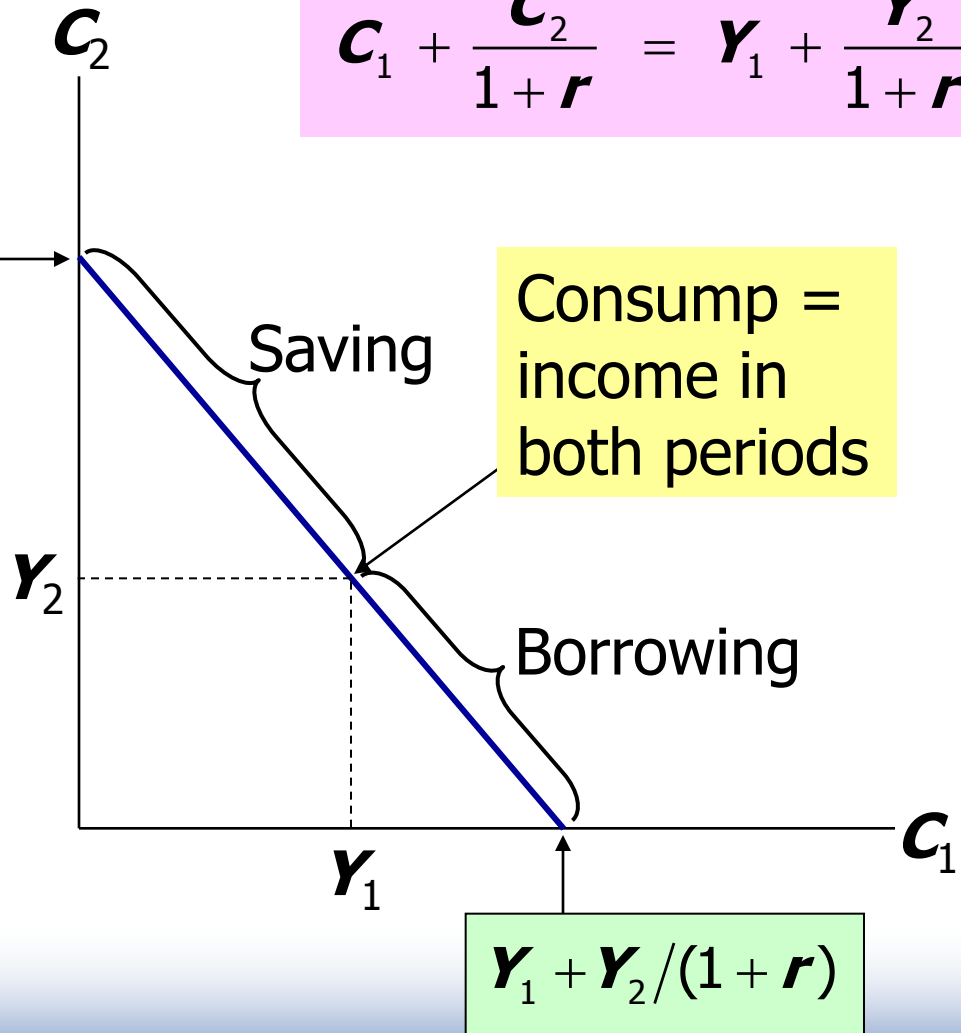
present value of  
lifetime income

# The intertemporal budget constraint

The budget constraint shows all combinations of  $C_1$  and  $C_2$  that just exhaust the consumer's resources.

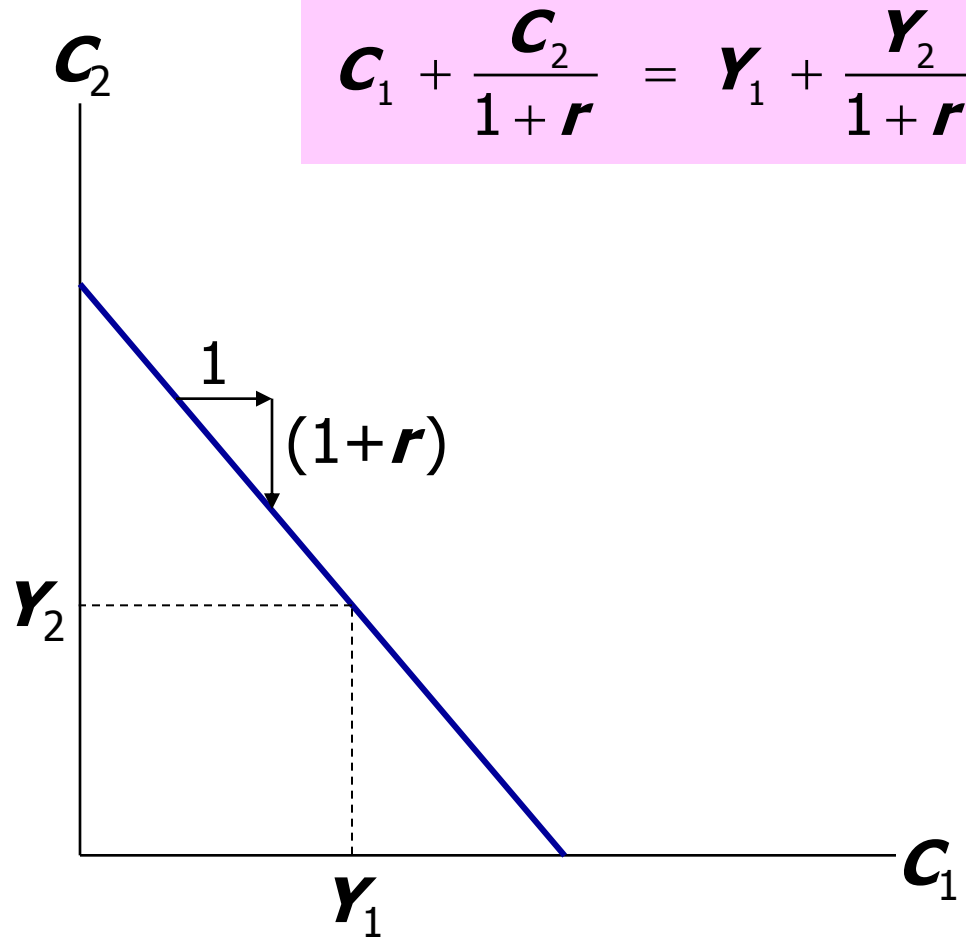
$$(1+r)Y_1 + Y_2$$

$$C_1 + \frac{C_2}{1+r} = Y_1 + \frac{Y_2}{1+r}$$



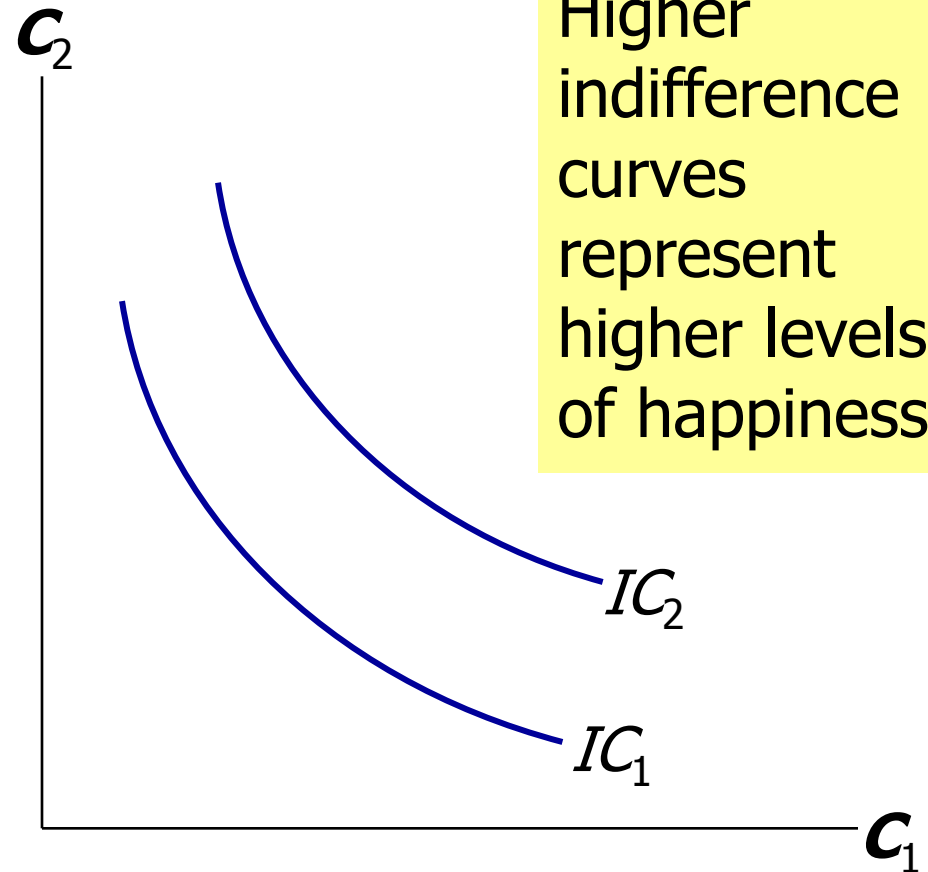
# The intertemporal budget constraint

The slope of the budget line equals  $-(1+r)$



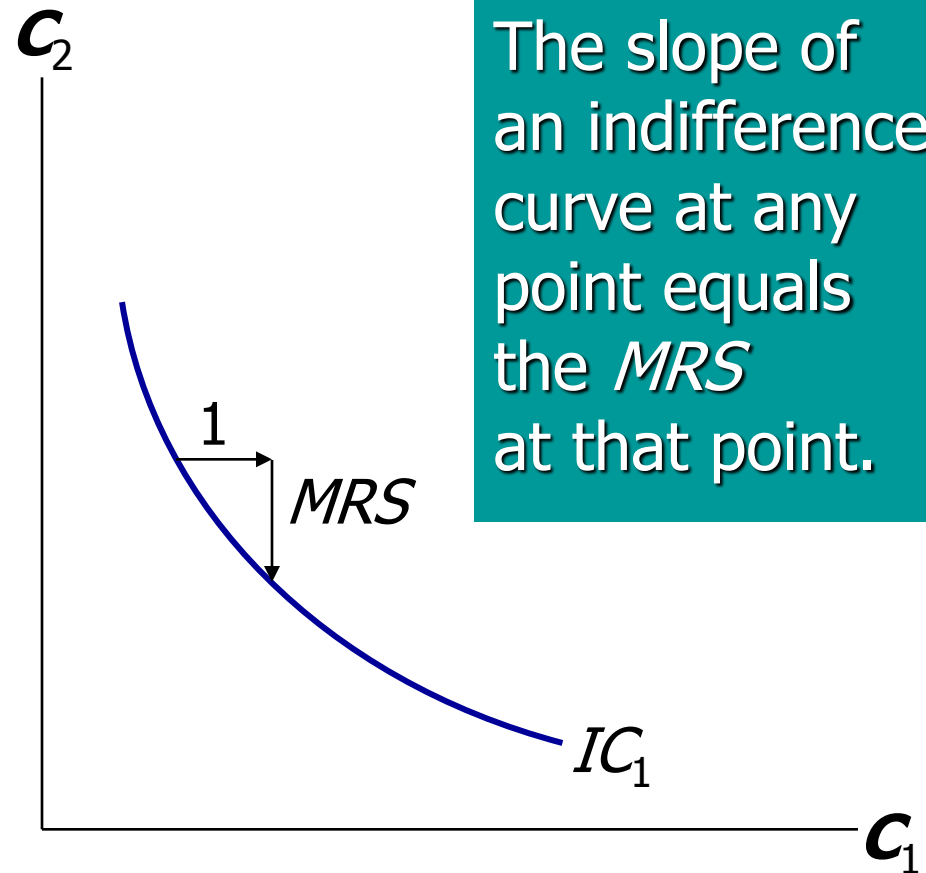
# Consumer preferences

An **indifference curve** shows all combinations of  $C_1$  and  $C_2$  that make the consumer equally happy.



# Consumer preferences

**Marginal rate of substitution (*MRS*):** the amount of  $C_2$  consumer would be willing to substitute for one unit of  $C_1$ .

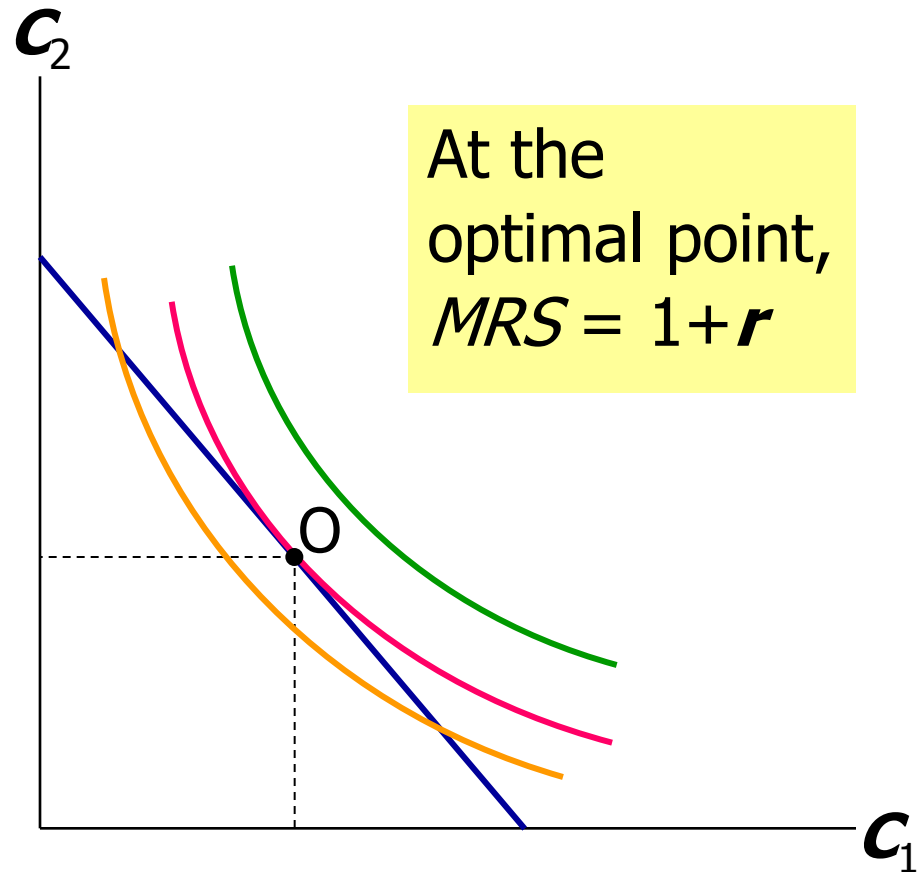


The slope of an indifference curve at any point equals the *MRS* at that point.



# Optimization

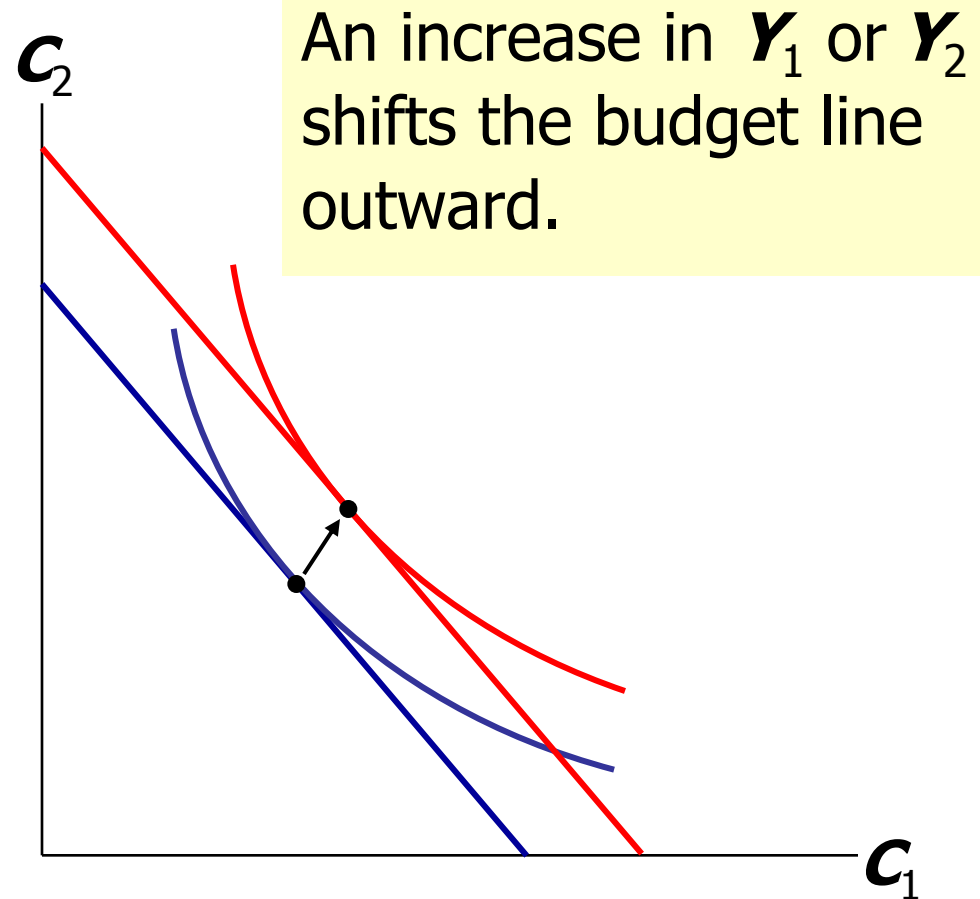
The optimal  $(C_1, C_2)$  is where the budget line just touches the highest indifference curve.



# How $C$ responds to changes in $Y$

Results:  
Provided they are  
both normal goods,  
 $C_1$  and  $C_2$  both  
increase,

*...regardless of  
whether the  
income increase  
occurs in period 1  
or period 2.*



# Keynes vs. Fisher

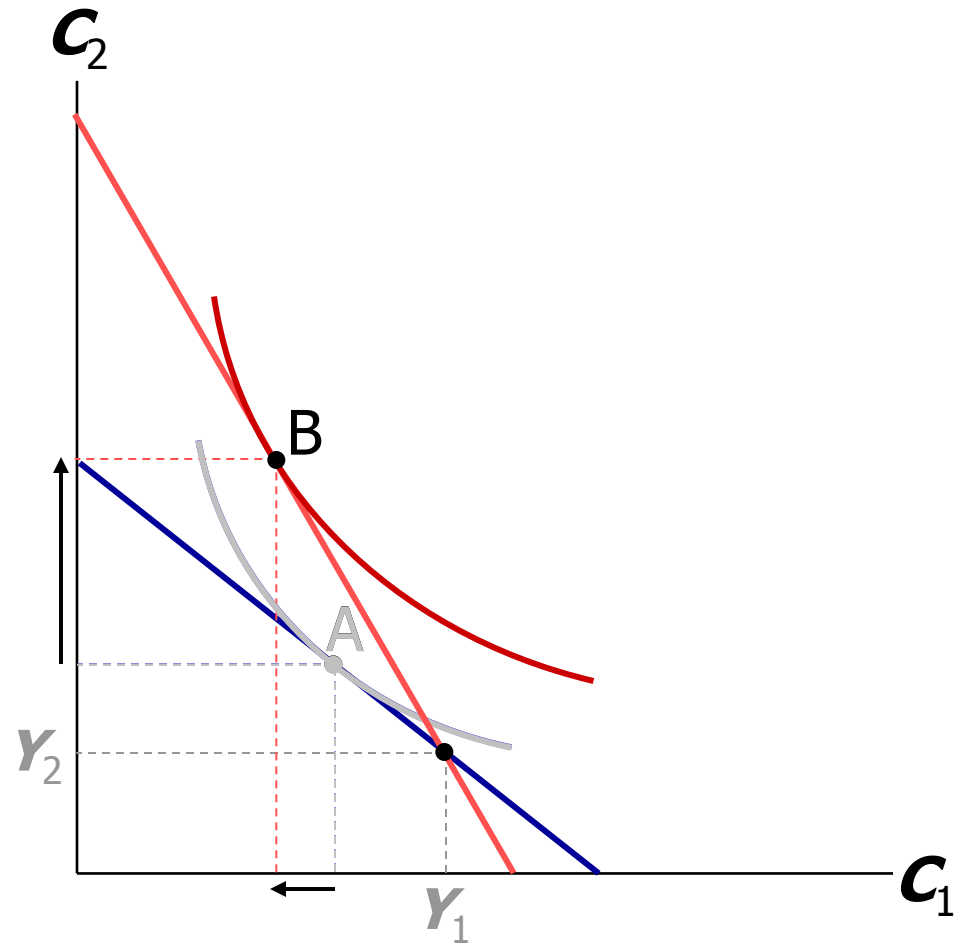
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- Keynes:  
current consumption depends only on current income
- Fisher:  
current consumption depends only on the present value of lifetime income;  
the timing of income is irrelevant  
because the consumer can borrow or lend between periods.

# How $C$ responds to changes in $r$

An increase in  $r$  pivots the budget line around the point  $(Y_1, Y_2)$ .

As depicted here,  $C_1$  falls and  $C_2$  rises. However, it could turn out differently...



# How $C$ responds to changes in $r$

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- income effect

If consumer is a saver, the rise in  $r$  makes him better off, which tends to increase consumption in both periods.

- substitution effect

The rise in  $r$  increases the opportunity cost of current consumption, which tends to reduce  $C_1$  and increase  $C_2$ .

- Both effects  $\Rightarrow \uparrow C_2$ .

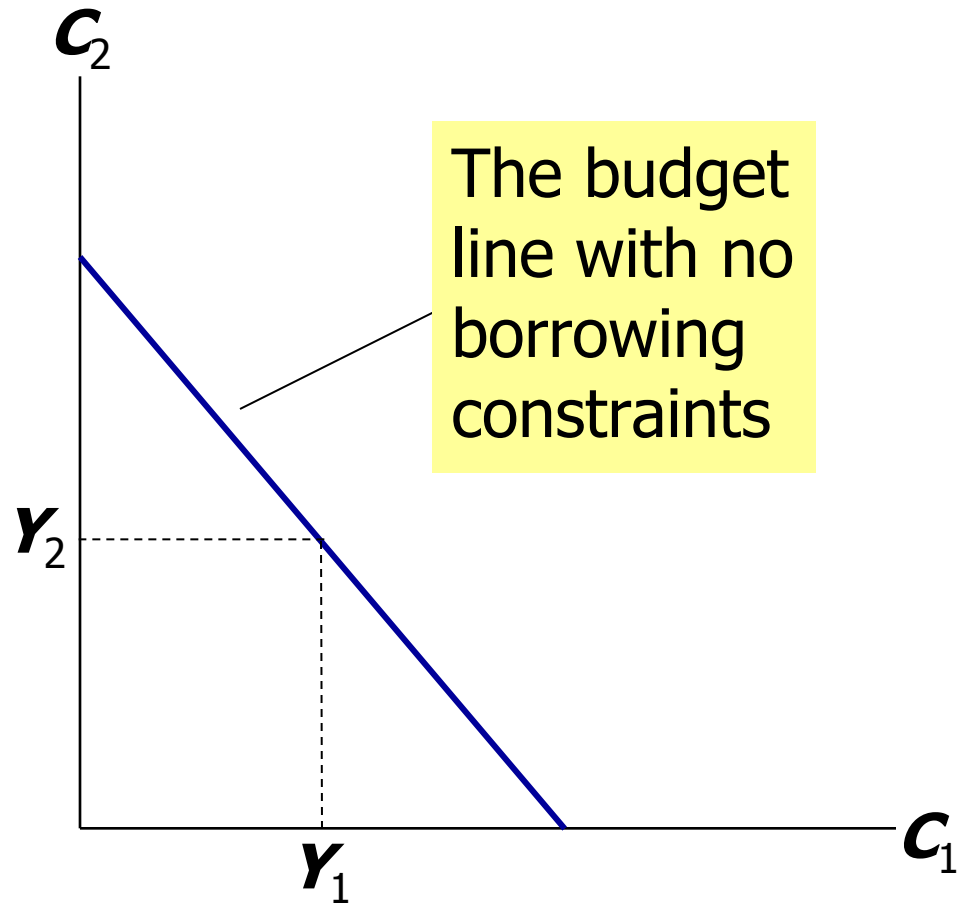
Whether  $C_1$  rises or falls depends on the relative size of the income & substitution effects.

# Constraints on borrowing

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- In Fisher's theory, the timing of income is irrelevant because the consumer can borrow and lend across periods.
- Example: If consumer learns that her future income will increase, she can spread the extra consumption over both periods by borrowing in the current period.
- However, if consumer faces **borrowing constraints** (aka "liquidity constraints"), then she may not be able to increase current consumption and her consumption may behave as in the Keynesian theory even though she is rational & forward-looking

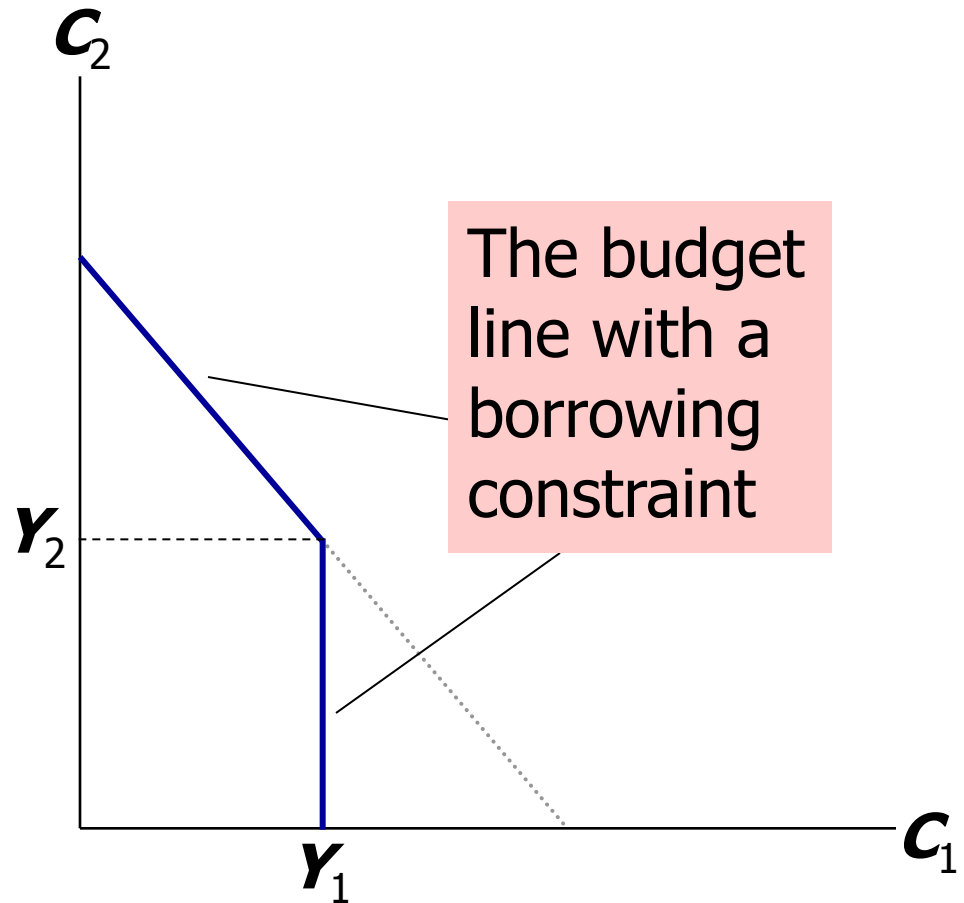
# Constraints on borrowing



# Constraints on borrowing

The borrowing constraint takes the form:

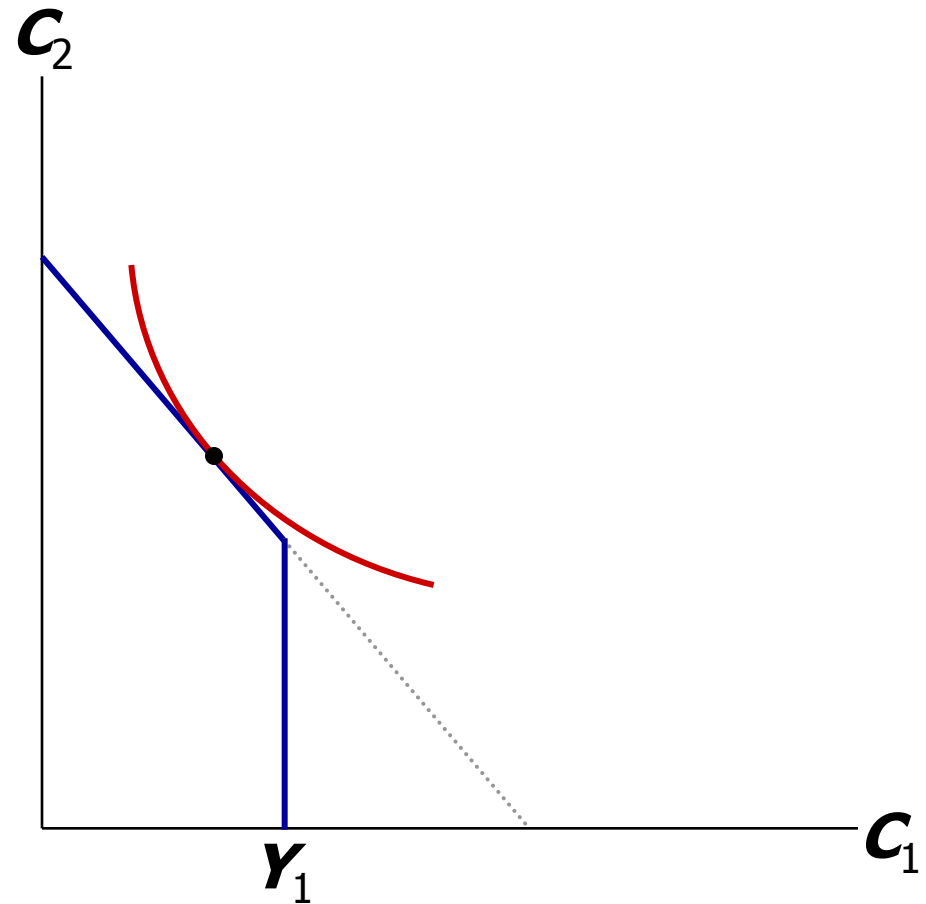
$$C_1 \leq Y_1$$





# Consumer optimization when the borrowing constraint is **not binding**

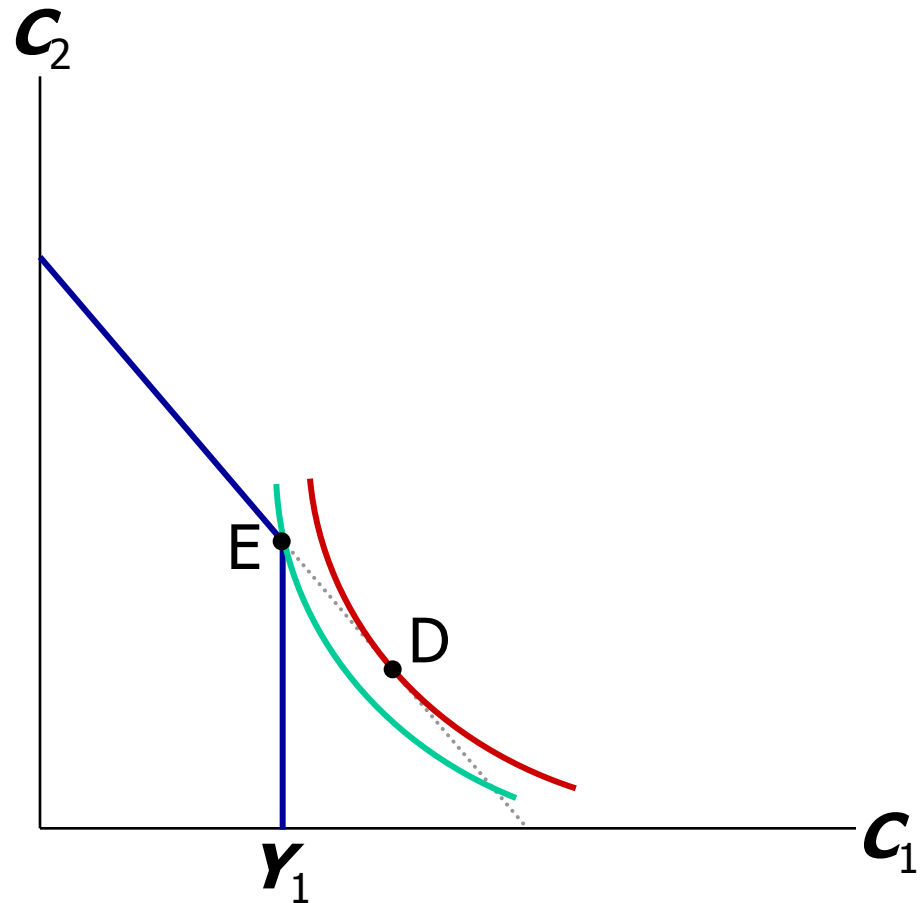
The borrowing constraint is not binding if the consumer's optimal  $C_1$  is less than  $Y_1$ .



# Consumer optimization when the borrowing constraint is binding

The optimal choice is at point D.

But since the consumer cannot borrow, the best he can do is point E.



# The Life-Cycle Hypothesis

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- due to Franco Modigliani (1950s)
- Fisher's model says that consumption depends on lifetime income, and people try to achieve smooth consumption.
- The LCH says that income varies systematically over the phases of the consumer's "life cycle," and saving allows the consumer to achieve smooth consumption.

# The Life-Cycle Hypothesis

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- The basic model:

**$W$**  = initial wealth

**$Y$**  = annual income until retirement  
(assumed constant)

**$R$**  = number of years until retirement

**$T$**  = lifetime in years

- Assumptions:

- zero real interest rate (for simplicity)
- consumption-smoothing is optimal

# The Life-Cycle Hypothesis

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- Lifetime resources =  $W + RY$
- To achieve smooth consumption, consumer divides her resources equally over time:

$$C = (W + RY)/T, \text{ or}$$

$$C = \alpha W + \beta Y$$

where

$\alpha = (1/T)$  is the marginal propensity to consume out of wealth

$\beta = (R/T)$  is the marginal propensity to consume out of income

# Implications of the Life-Cycle Hypothesis

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The Life-Cycle Hypothesis can solve the consumption puzzle:

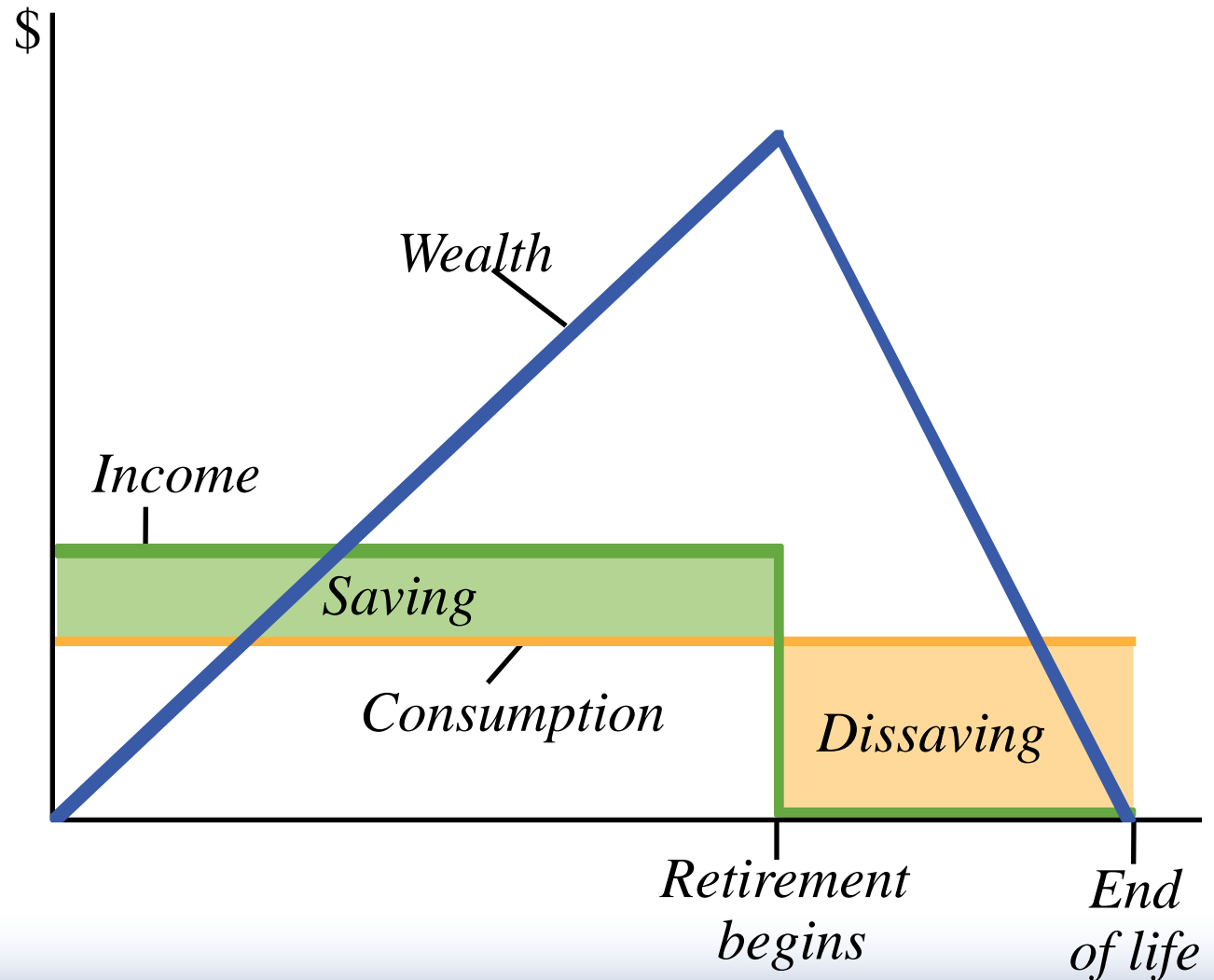
- The *APC* implied by the life-cycle consumption function is

$$C/Y = \alpha(W/Y) + \beta$$

- Across households, wealth does not vary as much as income, so high income households should have a lower APC than low income households.
- Over time, aggregate wealth and income grow together, causing APC to remain stable.

# Implications of the Life-Cycle Hypothesis

The LCH implies that saving varies systematically over a person's lifetime.



# The Permanent Income Hypothesis

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- due to Milton Friedman (1957)
- The PIH views current income  $Y$  as the sum of two components:
  - permanent income  $Y^P$   
(average income, which people expect to persist into the future)
  - transitory income  $Y^T$   
(temporary deviations from average income)



# The Permanent Income Hypothesis

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- Consumers use saving & borrowing to smooth consumption in response to transitory changes in income.
- The PIH consumption function:

$$C = \alpha Y^P$$

where  $\alpha$  is the fraction of permanent income that people consume per year.

# The Permanent Income Hypothesis

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The PIH can solve the consumption puzzle:

- The PIH implies

$$APC = C/Y = \alpha Y^P / Y$$

- To the extent that high income households have higher transitory income than low income households, the APC will be lower in high income households.
- Over the long run, income variation is due mainly if not solely to variation in permanent income, which implies a stable *APC*.

# PIH vs. LCH

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- In both, people try to achieve smooth consumption in the face of changing current income.
- In the LCH, current income changes systematically as people move through their life cycle.
- In the PIH, current income is subject to random, transitory fluctuations.
- Both hypotheses can explain the consumption puzzle.

# *Summing up*

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- Keynes suggested that consumption depends primarily on current income.
- Recent work suggests instead that consumption depends on
  - current income
  - expected future income
  - wealth
  - interest rates
- Economists disagree over the relative importance of these factors and of borrowing constraints and psychological factors.

# Chapter summary

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## 1. Keynesian consumption theory

- Keynes' conjectures
  - $MPC$  is between 0 and 1
  - $APC$  falls as income rises
  - current income is the main determinant of current consumption
- Empirical studies
  - in household data & short time series: confirmation of Keynes' conjectures
  - in long time series data:  
 $APC$  does not fall as income rises

# Chapter summary

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2. Fisher's theory of intertemporal choice
  - Consumer chooses current & future consumption to maximize lifetime satisfaction subject to an intertemporal budget constraint.
  - Current consumption depends on lifetime income, not current income, provided consumer can borrow & save.
3. Modigliani's Life-Cycle Hypothesis
  - Income varies systematically over a lifetime.
  - Consumers use saving & borrowing to smooth consumption.
  - Consumption depends on income & wealth.

# Chapter summary

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4. Friedman's Permanent-Income Hypothesis
  - Consumption depends mainly on permanent income.
  - Consumers use saving & borrowing to smooth consumption in the face of transitory fluctuations in income.